



# Multi-level Contrastive Learning Framework for Sequential Recommendation

Ziyang Wang\*  
CCIIP Laboratory, Huazhong  
University of Science and Technology  
Alibaba Group  
China  
ziyang1997@hust.edu.cn

Huoyu Liu\*  
Alibaba Group  
China  
huoyu.lhy@alibaba-inc.com

Wei Wei†  
CCIIP Laboratory, Huazhong  
University of Science and Technology  
Joint Laboratory of HUST and Pingan  
Property & Casualty Research (HPL)  
China  
weiw@hust.edu.cn

Yue Hu  
Alibaba Group  
China  
lingshu.hy@alibaba-inc.com

Xian-Ling Mao  
Beijing Institute of Technology  
China  
maoxl@bit.edu.cn

Shaojian He  
Alibaba Group  
China  
shaojian.he@alibaba-inc.com

Rui Fang  
Ping An Property & Casualty  
Insurance company of China, Ltd  
China  
fangrui051@pingan.com.cn

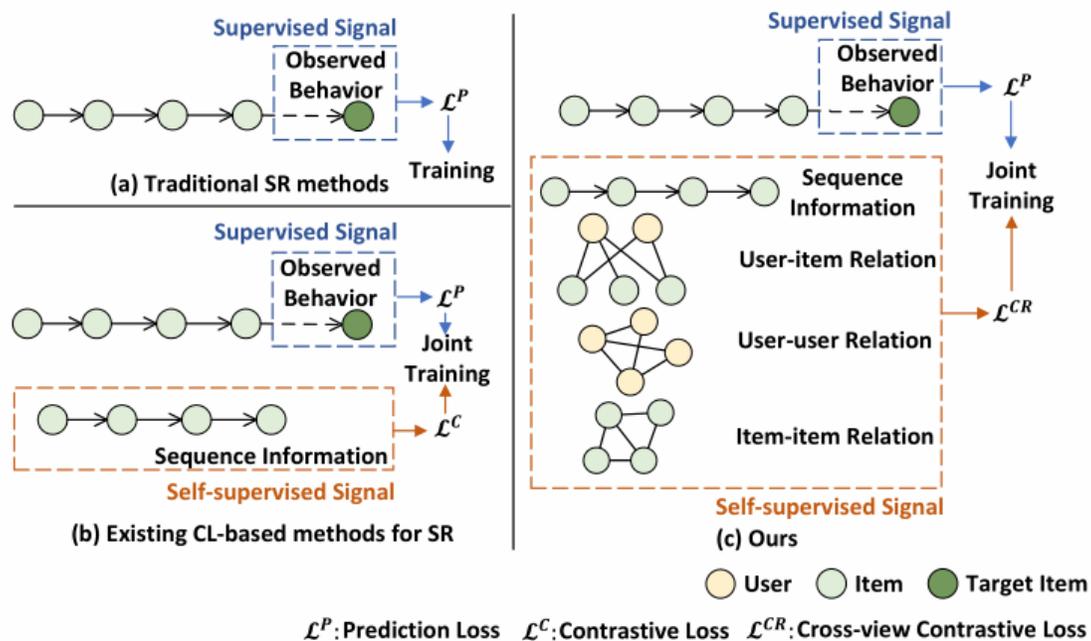
Dangyang Chen  
Ping An Property & Casualty  
Insurance company of China, Ltd  
China  
chendangyang273@pingan.com.cn



CIKM 2022

Reported by Nengqiang Xiang

# Introduction



**Figure 1: Illustration of training mechanisms of different methods for SR. (a) Traditional methods for SR where the supervised signals are entirely based on the observed user behaviors. (b) Recently contrastive learning-based methods for SR learn the self-supervised signals from the sequence itself. (c) Our proposed method learns rich self-supervised signals by performing cross-view contrastive learning on sequence information, user-item, user-user, and item-item relations.**

Each behavior sequence contains a limited number of items, and the self-monitoring information obtained from the sequence is insufficient.

By simply enhancing the data of the behavior sequence, a comparison pair is generated, resulting in low information diversity of the comparison pair.

This paper propose a multi-level contrastive learning framework for sequential recommendation (MCLSR).

# Method

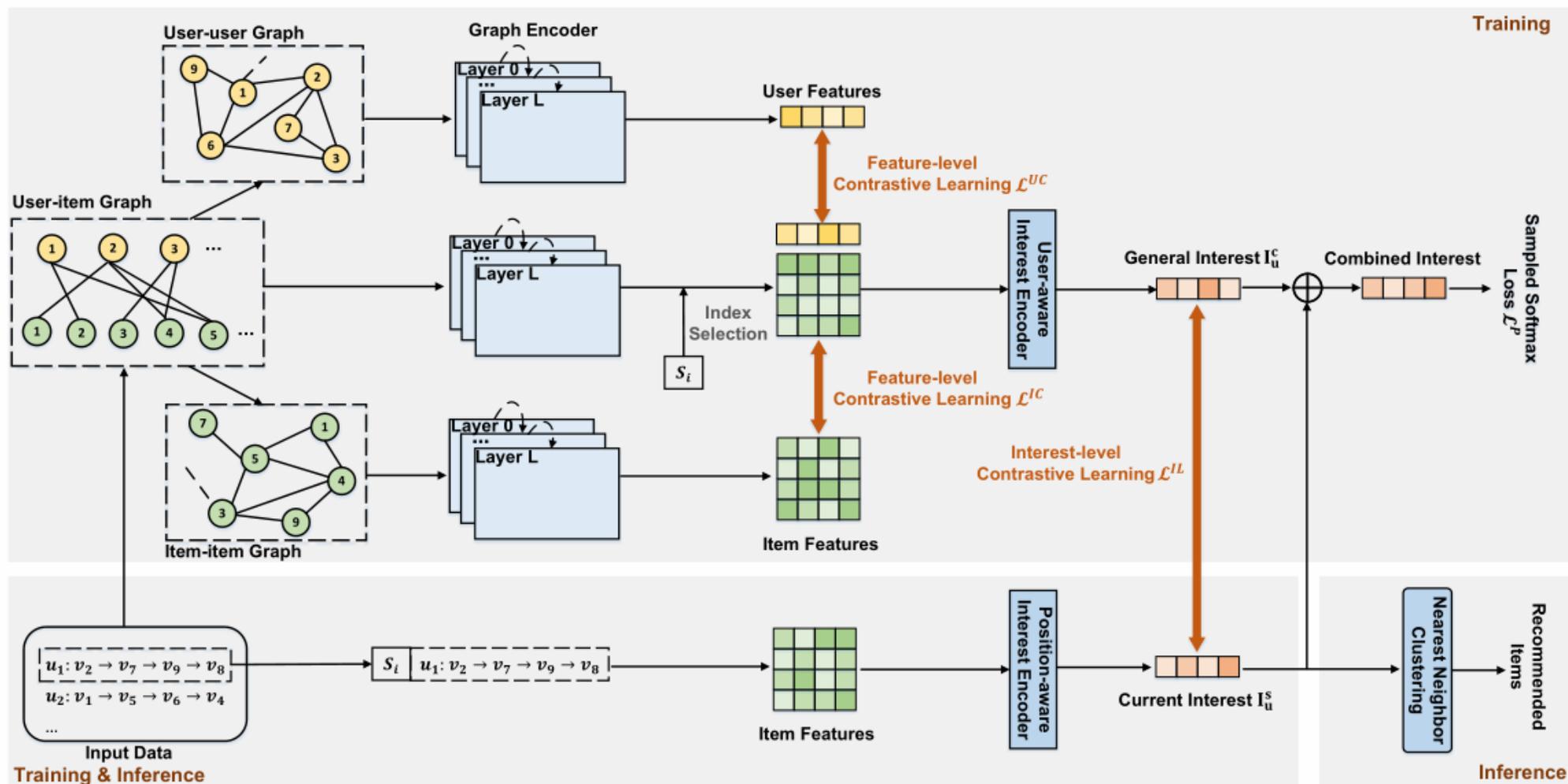
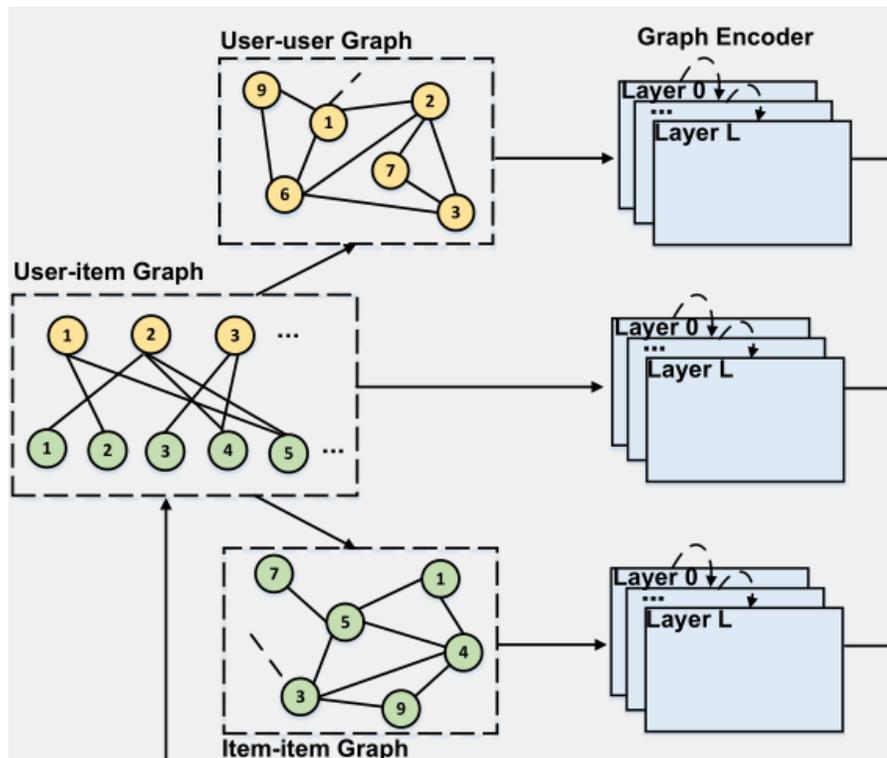


Figure 2: An overview of the proposed framework.  $\oplus$  denotes the element-wise summation.

## Method



### Problem Formulation:

$u \in \mathcal{U}$  : users set

$$\mathcal{M}^{uv} \in \mathbb{R}^{|\mathcal{U}| \times |\mathcal{V}|}$$

$v \in \mathcal{V}$  : items set

$$\mathcal{S}^{(u)} = \{v_1^{(u)}, v_2^{(u)}, \dots, v_{|S|}^{(u)}\}$$

$H^u \in \mathbb{R}^{|\mathcal{U}| \times d}$  : user embedding matrix

$H^v \in \mathbb{R}^{|\mathcal{V}| \times d}$  : item embedding matrix

### Graph Construction :

User-item graph:

$$\mathcal{G}^{uv} = (\mathcal{V}^{uv}, \mathcal{E}^{uv})$$

User-user graph:

$$\mathcal{G}^{uu} = (\mathcal{V}^{uu}, \mathcal{E}^{uu})$$

item-item graph :

$$\mathcal{G}^{vv} = (\mathcal{V}^{vv}, \mathcal{E}^{vv})$$

### Graph Encoder Layer:

$$X^{(l)} = \text{GraphEncoder}(X, A) = D^{-\frac{1}{2}} A D^{-\frac{1}{2}} X^{(l-1)}, \quad (1)$$

# Method

## Interest-level Contrastive Learning :

### Current interest learning :

$$A^S = \text{softmax} \left( W_2 \tanh(W_1 (E^{u,p})^T) \right), \quad (2)$$

$$E^{u,p} = [h_1^v + p_1, h_2^v + p_2, \dots, h_n^v + p_n]$$

$$I_u^S = A^S E^u. \quad (3)$$

$$E^u = [h_1^v, h_2^v, \dots, h_n^v]$$

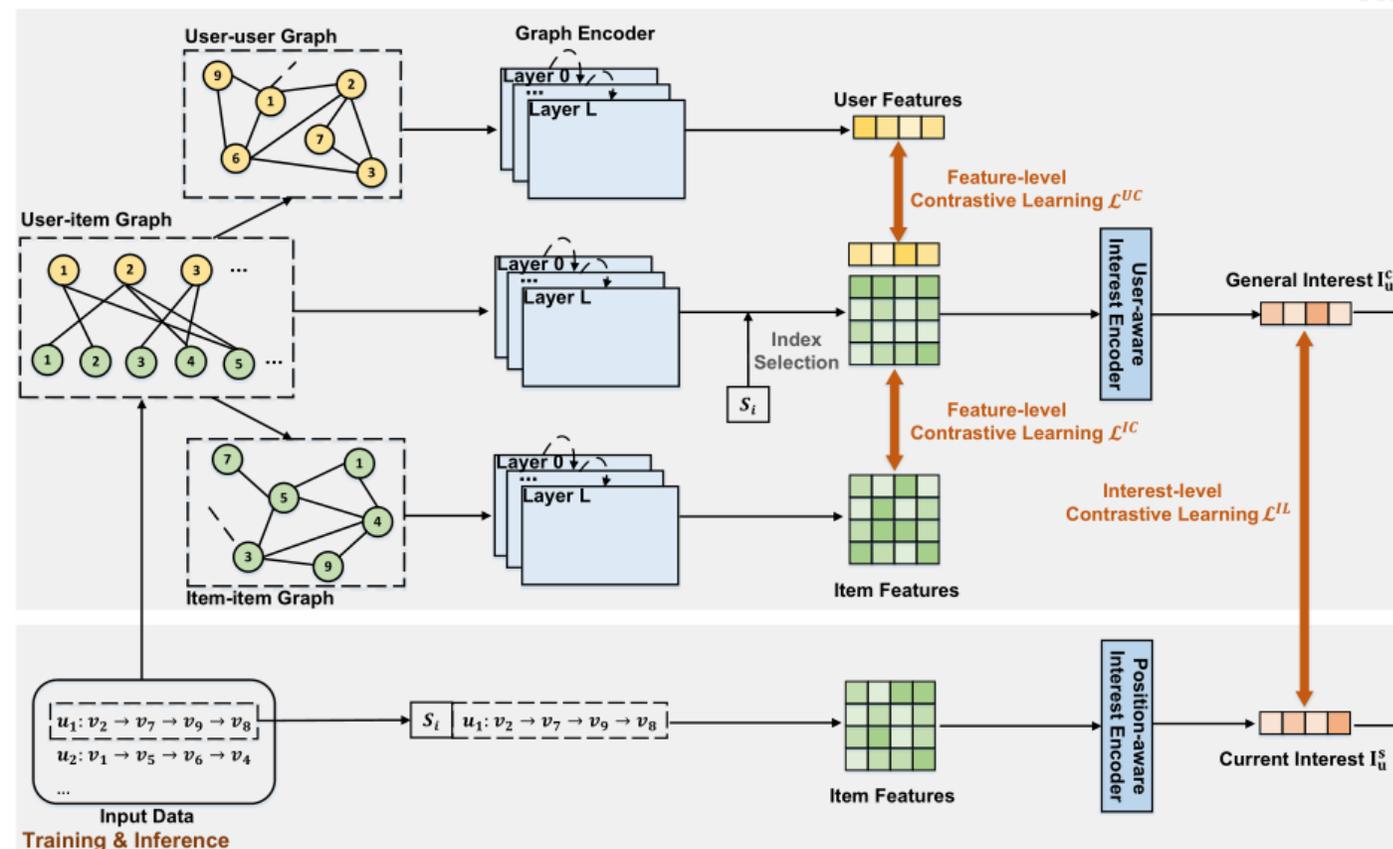
### General interest learning :

$$H^{all,uv} = \text{GraphEncoder}^{(l)}(H^{all}, \mathcal{G}^{uv}), \quad (4)$$

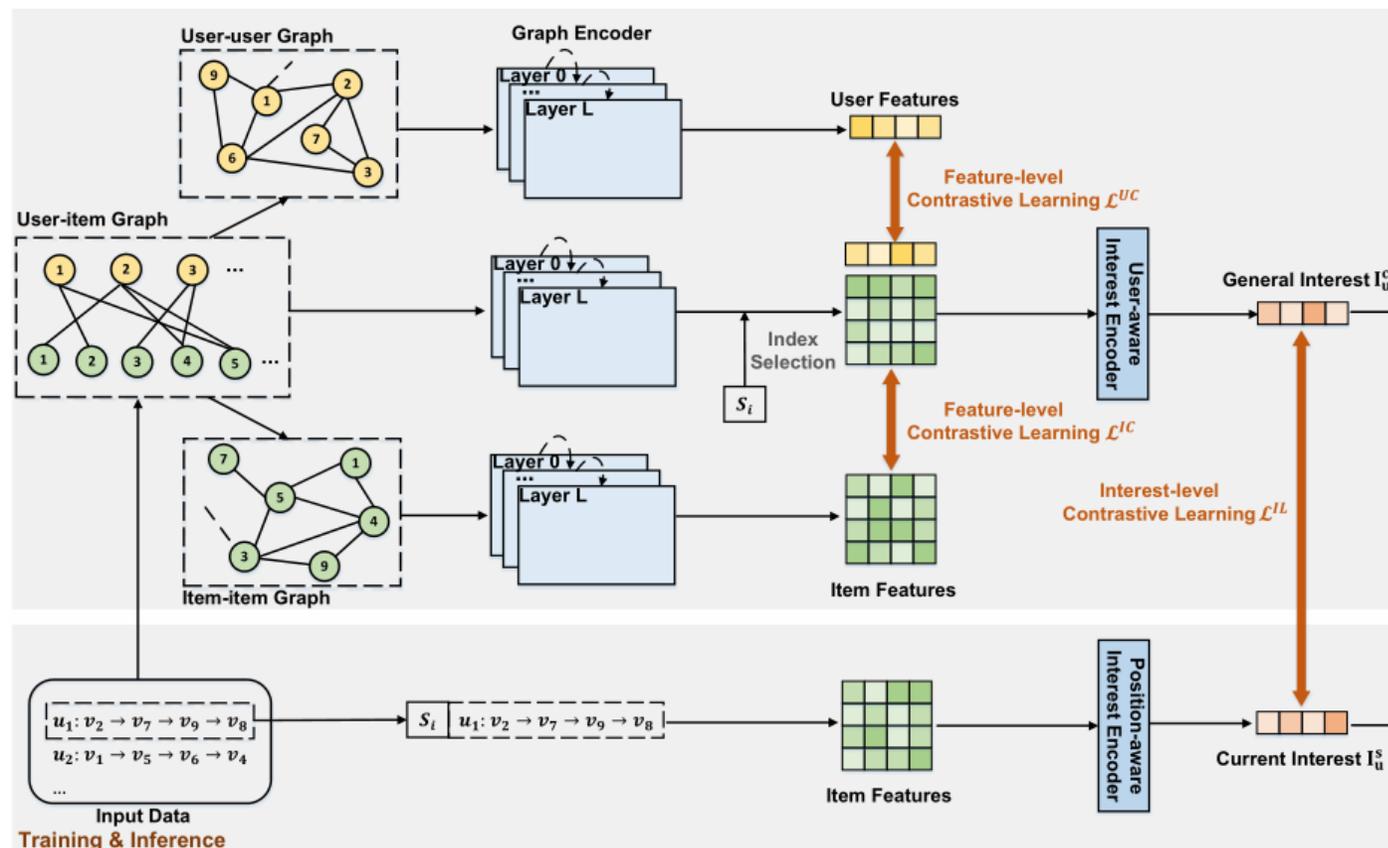
$$H^{all} = [H^u || H^v]$$

$$A^C = \text{softmax} \left( \tanh(W_3 h^{u,uv}) (E^{u,uv})^T \right), \quad (5)$$

$$I_u^C = A^C E^{u,uv}. \quad (6)$$



# Method



**Cross-view contrastive learning:**

$$\mathbf{T}^{I,s} = \left( \mathbf{W}_2^p \sigma(\mathbf{W}_1^p \mathbf{I}_u^s + \mathbf{b}_1^p) + \mathbf{b}_2^p \right), \quad (7)$$

$$\mathbf{T}^{I,c} = \left( \mathbf{W}_2^p \sigma(\mathbf{W}_1^p \mathbf{I}_u^c + \mathbf{b}_1^p) + \mathbf{b}_2^p \right),$$

$$\mathcal{L}^{IL} = \sum_{i=1} -\log \frac{\Psi(\mathbf{T}_i^{I,s}, \mathbf{T}_i^{I,c})}{\sum_j \Psi(\mathbf{T}_i^{I,s}, \mathbf{T}_j^{I,c}) + \sum_{j \neq i} \Psi(\mathbf{T}_i^{I,s}, \mathbf{T}_j^{I,s})}, \quad (8)$$

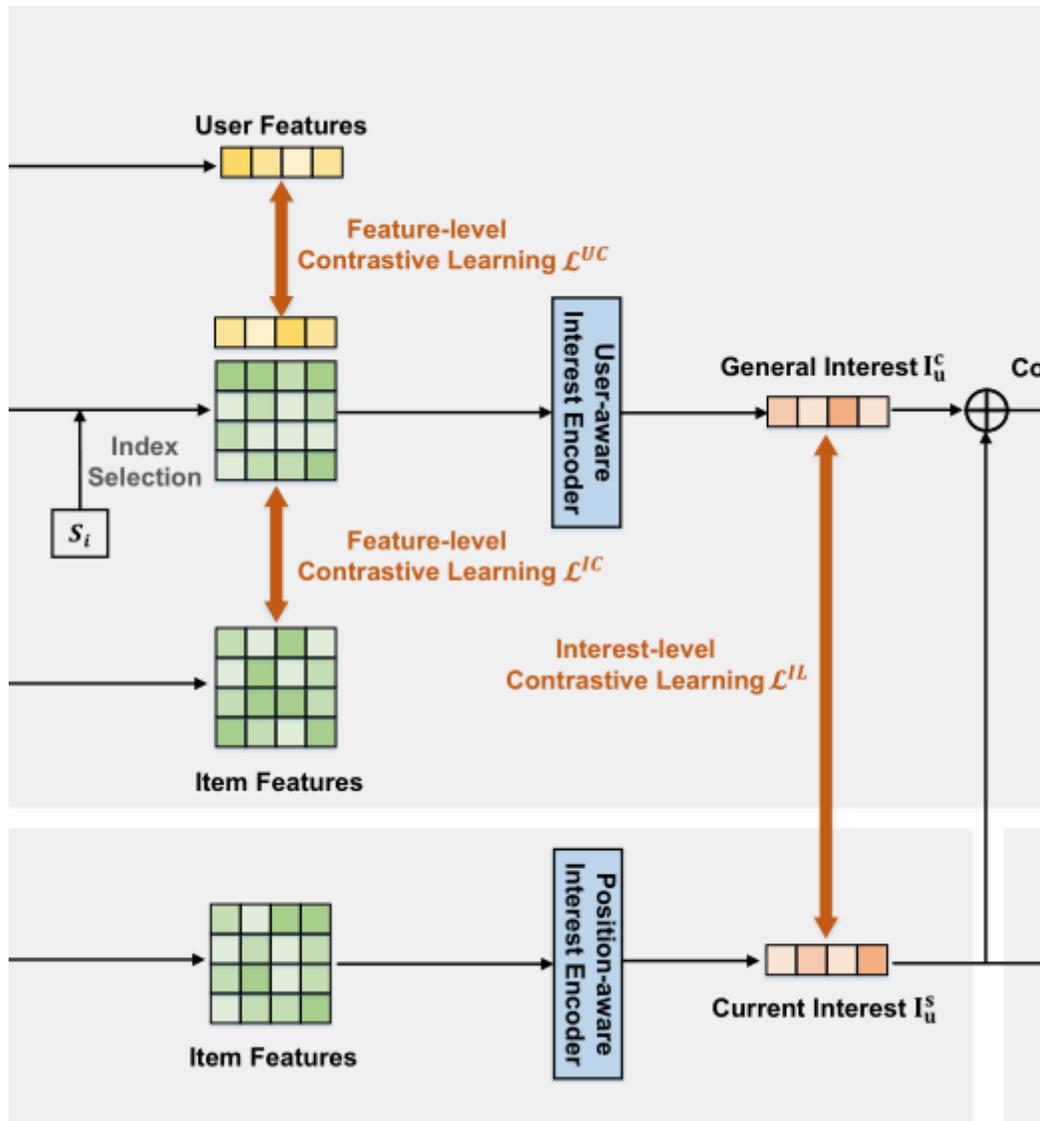
**Feature-level Contrastive Learning:**

**Feature learning:**

$$[\mathbf{H}^{u,uv} || \mathbf{H}^{v,uv}] = \text{GraphEncoder}^{(l)}([\mathbf{H}^u || \mathbf{H}^v], \mathcal{G}^{uv}), \quad (9)$$

$$\mathbf{H}^{u,uu} = \text{GraphEncoder}^{(l)}(\mathbf{H}^u, \mathcal{G}^{uu}),$$

## Method



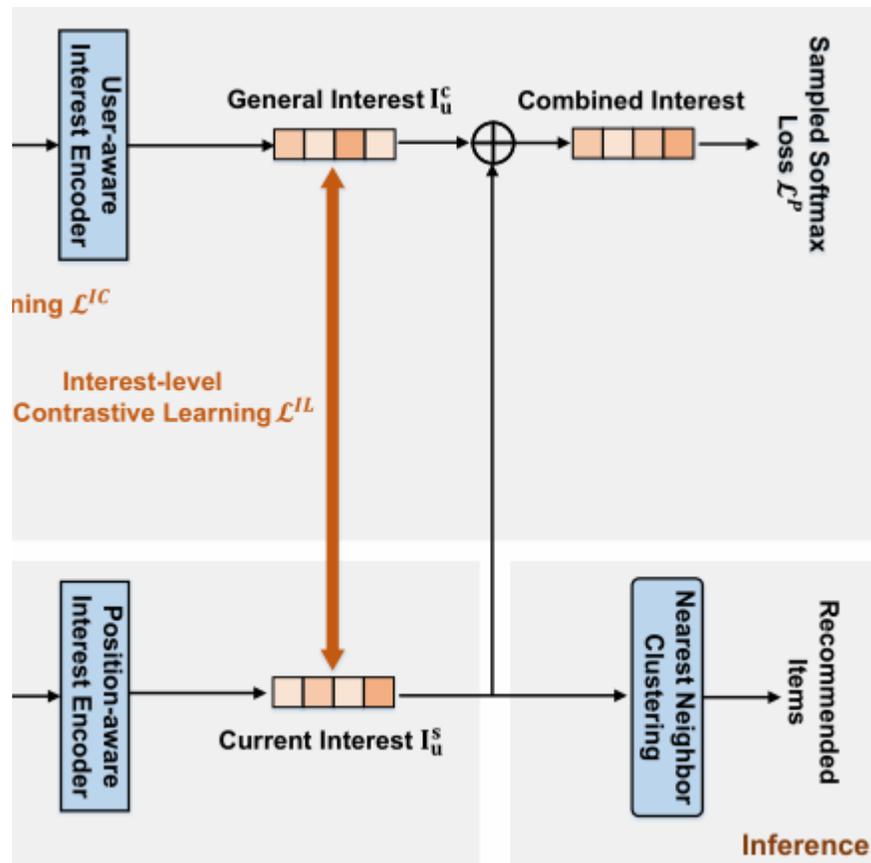
**Cross-view contrastive learning:**

$$\begin{aligned} \mathbf{T}^{F,uu} &= \mathbf{W}_4^p \sigma(\mathbf{W}_3^p \mathbf{H}^{u,uu} + \mathbf{b}_3^p) + \mathbf{b}_4^p, \\ \mathbf{T}^{F,uv} &= \mathbf{W}_4^p \sigma(\mathbf{W}_3^p \mathbf{H}^{u,uv} + \mathbf{b}_3^p) + \mathbf{b}_4^p, \end{aligned} \quad (10)$$

$$\mathcal{L}^{UC} = \sum_{i=1} -\log \frac{\Psi(\mathbf{T}_i^{F,uv}, \mathbf{T}_i^{F,uu})}{\sum_j \Psi(\mathbf{T}_i^{F,uv}, \mathbf{T}_j^{F,uu}) + \sum_{j \neq i} \Psi(\mathbf{T}_i^{F,uv}, \mathbf{T}_j^{F,uv})}, \quad (11)$$

$$\mathcal{L}^{FL} = \mathcal{L}^{UC} + \mathcal{L}^{IC}. \quad (12)$$

## Method



### Training and Inference:

#### Training phase:

$$\mathbf{I}_u^{comb} = \alpha \mathbf{I}_u^s + (1 - \alpha) \mathbf{I}_u^c, \quad (13)$$

$$\mathcal{L}^P = \sum_{u \in U} -\log \frac{\exp((\mathbf{I}_u^{comb})^T \mathbf{h}_o^v)}{\sum_{k \in \text{Sample}(\mathcal{V})} \exp((\mathbf{I}_u^{comb})^T \mathbf{h}_k^v)}. \quad (14)$$

$$\mathcal{J}(\theta) = \mathcal{L}^P + \beta \mathcal{L}^{IL} + \gamma \mathcal{L}^{FL}, \quad (15)$$

#### Inference phase:

$$R(u, N) = \text{Top-N}_{v \in V} \left( (\mathbf{I}_u^s)^T \mathbf{h}_v \right), \quad (16)$$



# Experiments

**Table 1: Statistics of the used datasets.**

Dataset	# user	# item	# interactions	Avg. len.	Sparsity
Books	459,133	313,966	8,898,041	9.7	99.993%
Clothing	39,387	23,034	278,677	6.9	99.969%
Toys	75,258	64,444	1,097,592	9.6	99.977%
Gowalla	65,506	174,606	2,061,264	14.5	99.982%

## Experiments

**Table 2: Effectiveness comparison between MCLSR and state-of-the-art approaches. <sup>†</sup> denotes the performance improvement over the best baseline is statistically significant with p-value < 0.01.**

Datasets	Metric	POPRec	GRU4Rec	SASRec	ComiRec-SA	GCSAN	S <sup>3</sup> -Rec <sub>MIP</sub>	CL4SRec	DuoRec	MCLSR	Improv.
Books	Recall@20	1.368	3.787	6.274	5.489	5.721	6.336	6.544	<u>6.838</u>	<b>7.469<sup>†</sup></b>	9.2%
	NDCG@20	0.597	1.923	2.825	2.262	2.706	2.964	3.161	<u>3.257</u>	<b>3.479<sup>†</sup></b>	6.8%
	Hit@20	3.013	8.710	12.765	11.402	11.730	13.052	13.520	<u>14.173</u>	<b>15.542<sup>†</sup></b>	9.6%
	Recall@50	2.400	6.335	9.349	8.467	8.455	9.684	10.240	<u>10.826</u>	<b>11.583<sup>†</sup></b>	6.9%
	NDCG@50	0.826	2.600	3.627	3.082	3.434	3.894	4.113	<u>4.308</u>	<b>4.647<sup>†</sup></b>	7.9%
	Hit@50	5.219	13.597	18.547	17.202	16.865	19.142	20.170	<u>21.366</u>	<b>23.042<sup>†</sup></b>	7.8%
Clothing	Recall@20	1.200	1.623	2.646	1.678	2.242	2.704	2.863	<u>2.940</u>	<b>3.138<sup>†</sup></b>	6.7%
	NDCG@20	0.374	0.559	0.854	0.427	0.659	0.873	0.927	<u>1.018</u>	<b>1.081<sup>†</sup></b>	6.2%
	Hit@20	2.139	2.777	4.188	3.467	3.684	4.343	4.467	<u>4.829</u>	<b>5.138<sup>†</sup></b>	6.4%
	Recall@50	2.715	2.948	4.505	2.774	3.309	4.522	4.651	<u>4.956</u>	<b>5.352<sup>†</sup></b>	7.9%
	NDCG@50	0.640	0.778	1.151	0.723	0.829	1.116	1.199	<u>1.356</u>	<b>1.464<sup>†</sup></b>	8.0%
	Hit@50	4.833	5.085	6.705	5.052	5.812	6.723	7.155	<u>7.785</u>	<b>8.503<sup>†</sup></b>	9.2%
Toys	Recall@20	0.928	3.214	6.343	5.315	6.593	6.670	6.983	<u>7.841</u>	<b>8.254<sup>†</sup></b>	10.3%
	NDCG@20	0.510	1.641	2.912	2.114	2.817	3.073	3.072	<u>3.418</u>	<b>3.726<sup>†</sup></b>	9.0%
	Hit@20	2.496	6.926	12.838	11.075	13.153	13.474	14.079	<u>15.331</u>	<b>16.661<sup>†</sup></b>	8.7%
	Recall@50	1.844	5.406	10.264	8.962	10.018	10.730	11.300	<u>12.463</u>	<b>13.328<sup>†</sup></b>	6.9%
	NDCG@50	0.774	2.216	3.899	2.952	3.690	4.072	4.095	<u>4.612</u>	<b>5.081<sup>†</sup></b>	10.2%
	Hit@50	4.760	11.554	19.837	17.282	19.400	20.363	21.330	<u>23.389</u>	<b>25.462<sup>†</sup></b>	8.9%
Gowalla	Recall@20	1.206	5.642	8.581	5.559	7.869	7.823	8.804	<u>8.973</u>	<b>9.317<sup>†</sup></b>	3.8%
	NDCG@20	1.191	5.536	7.546	3.891	6.819	7.351	7.601	<u>7.618</u>	<b>7.759<sup>†</sup></b>	1.9%
	Hit@20	5.874	22.450	28.931	19.052	26.315	27.676	29.853	<u>30.075</u>	<b>31.832<sup>†</sup></b>	5.8%
	Recall@50	2.084	9.623	13.838	9.891	12.793	12.710	14.372	<u>15.195</u>	<b>15.972<sup>†</sup></b>	5.1%
	NDCG@50	1.678	7.784	10.510	5.725	9.107	9.752	10.630	<u>10.735</u>	<b>11.012<sup>†</sup></b>	2.6%
	Hit@50	9.716	34.321	42.380	32.041	38.613	39.463	43.659	<u>44.618</u>	<b>46.217<sup>†</sup></b>	3.5%

# Experiments

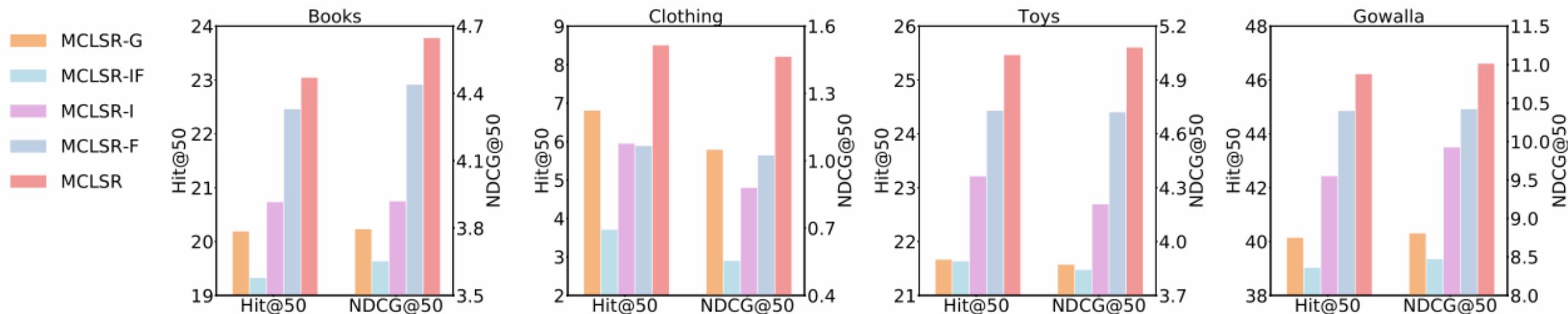
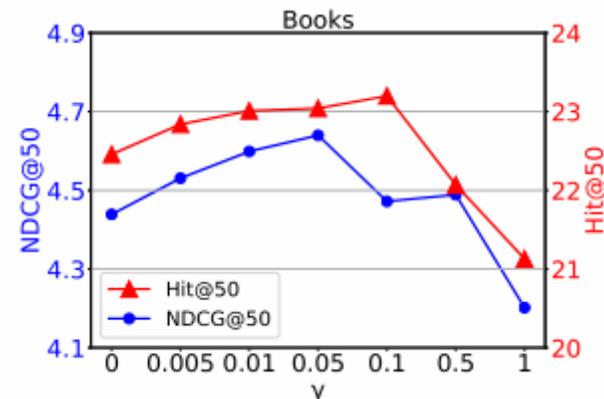
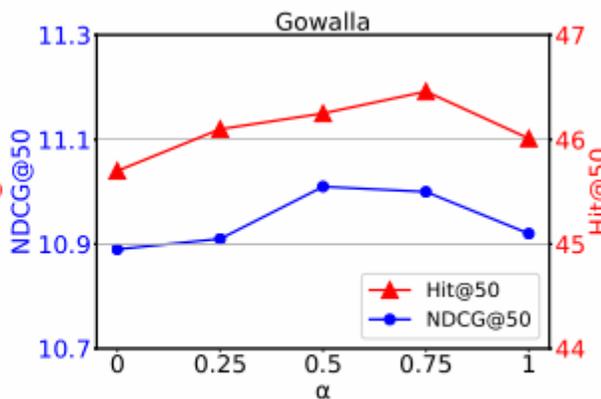
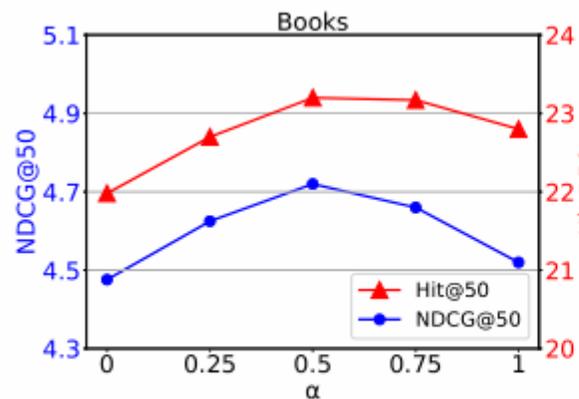


Figure 3: Ablation study on four datasets.

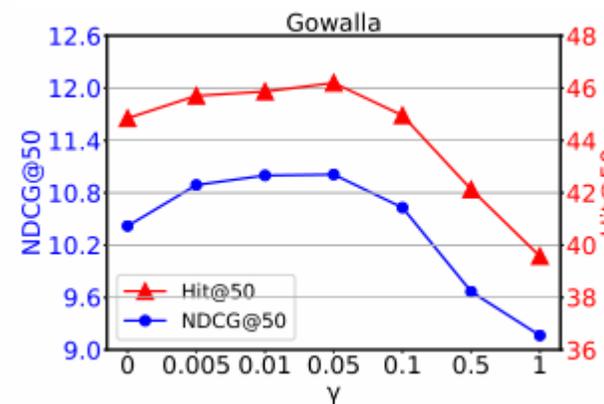
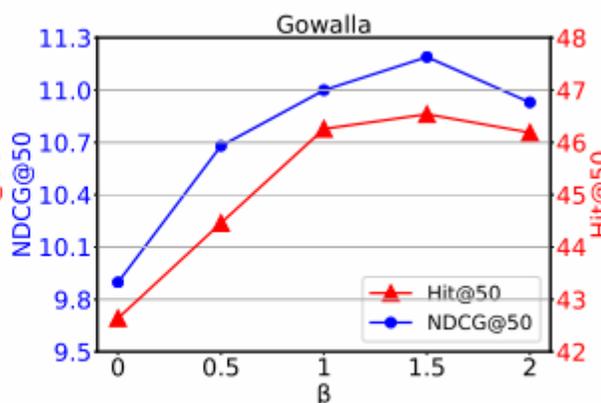
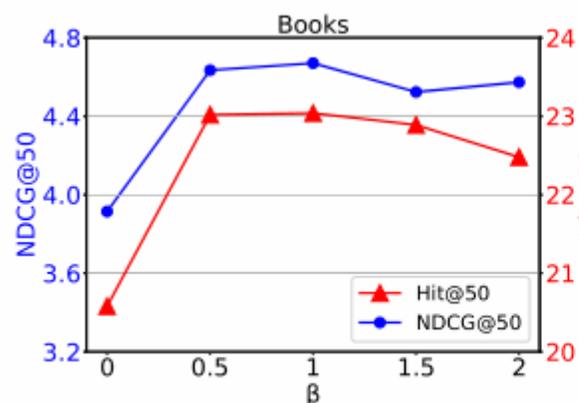
Table 3: The performance of MCLSR with varied depth of GNN layers in terms of Metrics@50.

Depth	Books			Clothing			Toys			Gowalla		
	Recall	NDCG	Hit Rate	Recall	NDCG	Hit Rate	Recall	NDCG	Hit Rate	Recall	NDCG	Hit Rate
$l = 0$	9.881	3.799	20.032	13.025	8.805	40.141	11.052	3.847	21.673	13.265	8.728	40.273
$l = 1$	10.853	4.166	21.782	15.897	10.889	44.543	13.165	4.744	25.069	15.769	10.743	45.620
$l = 2$	<b>11.583</b>	<b>4.647</b>	<b>23.042</b>	<b>15.972</b>	<b>11.012</b>	<b>46.217</b>	13.328	5.081	25.462	<b>15.972</b>	<b>11.012</b>	<b>46.217</b>
$l = 3$	10.085	3.936	20.547	15.021	10.042	43.775	<b>13.720</b>	<b>5.187</b>	<b>26.417</b>	14.948	10.094	43.665

# Experiments



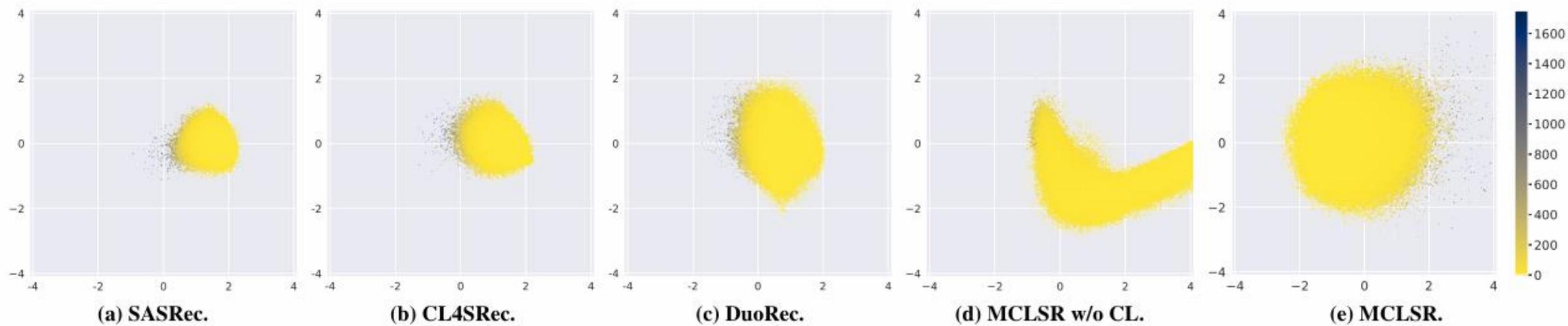
(a) Sensitive of parameter  $\alpha$



(b) Sensitive of parameter  $\beta$

(c) Sensitive of parameter  $\gamma$

# Experiments



**Figure 5: Item embeddings of selected methods on Book dataset.**



**Thanks**